

# NOVEL IMPLEMENTATION METHOD OF MODULO $2^N$ MULTIPLICATION FOR DIGITAL SIGNAL PROCESSING

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## RINGKASAN

Kertaskerja ini membentangkan satu cara baharu dalam mana satu pendaraf modulo  $2^N$  dijelmakan secara isomorfik menjadi sepasang penyampur modulo 2 dan modulo  $2^{N-2}$ . Bilangan penyampur-penyampur penuh yang diperlukan untuk pelaksanaan bertambah secara linear dengan bertambahnya panjang perkataan  $N$ , dan tidak dengan secara eksponen, dan kelewatan pengantaran sistem tetap pada asasnya tidak berubah dengan bertambahnya  $N$ .

## ABSTRACT

*This paper presents a novel method in which a modulo  $2^N$  multiplier is transformed isomorphically into a pair of modulo 2 and modulo  $2^{N-2}$  adders. The number of full-adders required for implementation increases linearly with increasing wordlength  $N$ , rather than exponentially, and the system propagation delay remains basically constant with increasing  $N$ .*

### 1. Introduction

In the past few years there has been an increasing application of number-theoretic concepts to digital signal processing<sup>1</sup>. In most signal processing algorithms the multiplier invariably forms one of the main computing elements, especially in hardware implementations in which component cost and processing speed are essential for efficient and economic hardware structures. In this paper, we present the main concepts and results of a novel technique with which a modulo  $2^N$  multiplier can be isomorphically transformed into a pair of modulo 2 and modulo  $2^{N-2}$  adders. It is shown that the number of full-adders required for their implementation increases linearly with increasing wordlengths  $N$  of the multiplier operands,

rather than exponentially as in most conventional implementations. Furthermore the system propagation delay is shown to remain basically constant with increasing  $N$ . The application of these results will lead to efficient and cost-effective hardware structures for modulo  $2^N$  multiplications.

## 2. Modulo $2^N$ Multiplication Using "Forced" Operands and Product Correction

The approach proposed is based on a *reduced* multiplier, which is the original modulo  $2^N$  multiplier whose operands and product are constrained to take on only the odd values from the set

$$Z_N = (0, 1, 2, \dots, 2^N - 1)$$

Hence, if  $A, B$  and  $A', B'$  are the operands to the original and reduced multipliers respectively, then  $A', B' \in Z_D$ , where

$$Z_D = \{x : x \text{ odd integer}, 1 \leq x \leq 2^N - 1\}.$$

These modified operands may be derived from the originals by the mapping  $g_A$  and  $g_B$ , where

$$g_A : A \rightarrow A' = A + c$$

$$\text{and } g_B : B \rightarrow B' = B + d$$

such that

$$c = \begin{cases} 0 & \text{for } A \text{ odd} \\ 1 & \text{for } A \text{ even} \end{cases} \quad d = \begin{cases} 0 & \text{for } B \text{ odd} \\ 1 & \text{for } B \text{ even} \end{cases}$$

Multiplying these 'forced' operands, we obtain,

$$\begin{aligned} P'_0 &\equiv A' \times B' \equiv (A + c)(B + d) \pmod{2^N} \\ &\equiv AB + dA + cB + cd \pmod{2^N} \end{aligned}$$

Hence the required product  $P_0 \equiv A \times B \pmod{2^N}$  is given by  $AB = (A' \times B') - (dA + cB + cd) \pmod{2^N}$ .

This congruence relationship expresses our proposed multiplication scheme, in which  $(A' \times B')$  describes the reduced multiplication and  $C = (dA + cB + cd)$  the correction required to obtain the actual product. The block diagram of the overall configuration is shown in Fig. 1.

The various values of  $C$  corresponding to all possible combinations of  $a$  and  $b$ , the L.S.B's of  $A$  and  $B$  respectively, are given below.

a	b	c	d	C
0	0	1	1	$A + B + 1$
0	1	1	0	$B$
1	0	0	1	$A$
1	1	0	0	$0$

This leads to a very simple correction circuit consisting of a modulo  $2^N$  adder which is just the conventional  $2^N$  adder with the carry digit excluded, and two gating circuits, each consisting of  $(N-1)$  2-input AND gates and one inverter. The output  $C$  from this correction unit is then subtracted from  $P'$  to obtain the actual product  $P_0$ .

## 3. Internal Algebraic Structure of Reduced Modulo $2^N$ Multipliers

In the following, we present only the main concepts and results of our study of the algebraic structure of a general reduced modulo  $2^N$  multiplier. The corresponding detailed arguments and proofs are in Ref. 2.

### 3.0 The group under modulo $2^N$ reduced multiplication

Let  $(Z_D, \otimes_{2^N})$  be the multiplier modulo  $2^N$  whose operands are constrained to odd values, i.e. from the set  $Z_D$ .

**Theorem 1:**— The set of odd integers, i.e.  $Z_D = \{x : x \text{ odd integer}, 1 \leq x \leq 2^N - 1\}$ , forms an Abelian group under multiplication modulo  $2^N$ . This group, which we denote by  $G(2^N)$ , has order  $G(2^N) = 2^{N-1}$ .

For the specific cases of our reduced multipliers moduli  $2^0, 2^1$  and  $2^2$ , we can prove, using elementary concepts in number theory (pages 123 to 125 in Ref. 2), that for each of these multipliers, its algebraic structure can be directly described and the complete multiplication table can be generated by a single element  $x \in Z_D$ , if  $x$  is a primitive root of  $2^N$ , where  $N = 0, 1$  or  $2$ .



### 3.1 Detailed algebraic structure of reduced modulo $2^N$ multipliers

In our following two lemmas and one theorem we extend the analysis to cases where  $N \geq 3$  and will show that the table of a general reduced modulo  $2^N$  multiplier,  $N \geq 3$ , can still be described completely but this time two elements  $Z_i, Z_j \in Z_D$  are required to generate it.

**Lemma 1:**—  $3^{2^N} = (2^{n+2})(x(n)) + 1$  for  $n \geq 1$  where  $x(n)$  is an odd number for all  $n$ .

**Corollary.** The element 3 in  $Z_{2^N}$  has order  $2^{N-2}$  in  $G(2^N)$ .

**Lemma 2:**— There are four elements,  $\pm 1$  and  $(2^{N-1} \pm 1)$ , in  $G(2^N)$  having order 2

**Corollary.** (a) The values  $x_h \equiv 1$  and  $x_i \equiv 2^{N-1}$

$+ 1$  (modulo  $2^N$ ) may be expressed as powers of 3 (modulo  $2^N$ ).  
(b) The values  $x_j \equiv -1$  and  $x_k \equiv 2^{N-1} - 1$  (modulo  $2^N$ ) cannot be powers of 3.

As a result of the above-mentioned Lemmas, the algebraic structure of our modified or reduced modulo  $2^N$  multiplier, for  $N \geq 3$ , can be described in detail via the following theorem.

**Theorem 2:**— The group  $G(2^N)$ , as described by Theorem 1, for  $N \geq 3$ , is isomorphic to the direct product group  $K \times H$ , where  $K$  and  $H$  are cyclic groups of orders  $2^{N-2}$  and 2 respectively.

The subgroup  $K$  is given by

$$K = (k_0, k_1, \dots, k_i, \dots, k_m), 0 \leq i < 2^{N-2},$$

$$m = 2^{N-2} - 1, k_i \in G(2^N) \text{ and } k_i = 3^i \text{ modulo } 2^N.$$

Thus subgroup  $L$  is given by  $L = (1_0, 1_i)$  where  $1_0, 1_i \in G(2^N)$  and

$$1_i \equiv x^i \text{ modulo } 2^N, \text{ for } i = 0, 1.$$

1. The value of  $x$  is either  $x \equiv -1$  modulo  $2^N$  or  $x \equiv 2^{N-1} - 1$  (see Corollary (b) of Lemma 2).

### 4. Application of Theoretical Results

The subgroups  $K$  and  $L$  may be used to organise  $G(2^N)$  by forming the relevant cosets in the usual way.

Let the cosets w.r.t.  $K$  be  $V_0$  and  $V_1$  and those w.r.t.  $L$  be  $W_0, W_1, \dots, W_i, \dots, W_n$ ,  $n = (2^{N-2} - 1)$ , given by

$$V_0 = (V_{0,0}, V_{0,1}, V_{0,2}, \dots, V_{0,i}, \dots, V_{0,n}) =$$

$$V_1 = (V_{1,0}, V_{1,1}, \dots, V_{1,i}, \dots, V_{1,n})$$

$$\text{and } W_0 = (W_{0,0}, W_{0,1}) = L, W_1 = (W_{1,0}, W_{1,1})$$

$$\dots, W_i = (W_{i,0}, W_{i,1}).$$

Where  $v_{d,i} = x^d 3^i$  modulo  $2^N$ ,  $d = 0$  or  $1$ ,  $0 \leq i \leq n$

and  $w_{i,d} = 3^i x^d$  modulo  $2^N$ , in which the value  $x$  is either  $x_j$  or  $x_k$  as described by Corollary (b) of Lemma 2.

In general, each element  $g_{1,m}$  of  $G(2^N)$  can be presented by the modulo  $2^N$  product of powers of  $x$  and 3 via the following congruence, i.e.

$$x^1 3^m = g_{1,m} \text{ modulo } 2^N, 1 \leq g_{1,m} \leq 2^N - 1,$$

where  $l = 0$  or  $1$  and  $0 \leq m < n$ .

From the corollary to Lemma 1, and the results in Lemma 2, the components  $3^m$  and  $x^1$ , will go through  $2^{N-2}$  and 2 values respectively before repeating themselves. Therefore this will generate  $(2^{N-2}) \times 2 = 2^{N-1}$  different elements of  $G(2^N)$ , the above congruence describes  $g_{1,m}$  uniquely.

Let us now express  $G(2^N)$  in terms of its cosets, i.e.  $G(2^N) = \{V_0; V_1\}$  using subgroup  $K$ , and  $G(2^N)$

$$= \{W_0; W_1; \dots; W_i; \dots; W_n\} \text{ using the subgroup } L.$$

If we consider any two elements of  $G(2^N)$ , say  $g_{1,m}$  and  $g_{1',m'}$ , then, it can be shown (Ref. 2)



that, their product P is given by  $P = g_{i,j}$  modulo  $2^N$ , where  $(1' + 1'') \equiv i$  modulo 2 and  $(m' + m'') \equiv j$  modulo  $2^{N-2}$ .

Since the subscripts I and m denote the cosets w.r.t. the subgroups K and L respectively, then we know that  $g_{1', m'} \in V_{1'}$ , and also  $W_{m'}$ ; and  $g_{1'', m''} \in V_{1''}$ , and also  $W_{m''}$ .

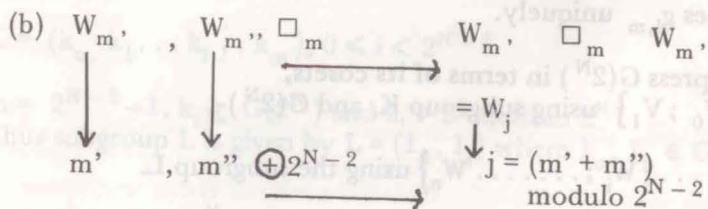
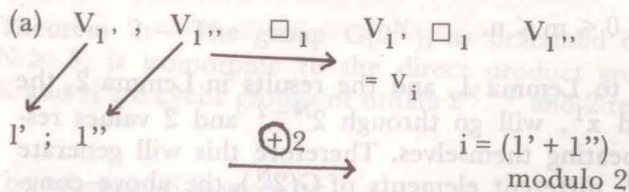
Furthermore, their modulo  $2^N$  product  $g_{i,j}$  belongs to both cosets  $V_i$  and  $W_j$  where i and j are the modulo 2, and modulo  $2^{N-2}$  sums of  $1', 1''$ , and  $m', m''$  respectively.

Consequently, if we denote the operation (i.e. multiplication) between any two cosets (w.r.t.K) by  $\square_1$  and that between any two (w.r.t.) by  $\square_m$  then it is not difficult to see that

$$V_{1'} \square_1 V_{1''} = V_{(1'+1'')} \text{ modulo 2, and } W_{m'} \square_m W_{m''} = W_{(m'+m'')} \text{ modulo } 2^{N-2}$$

In other words, if each coset is mapped onto its corresponding index, i.e.  $V_{1'} \rightarrow 1', V_{1''} \rightarrow 1''$  and

$W_{m'} \rightarrow m', W_{m''} \rightarrow m''$ . Then operations between cosets may be mapped onto modulo addition operations between indices as shown by the two commutative diagrams below.



Finally, the complete reduced modulo  $2^N$  multiplication may be described in a compact way as follows.

Let  $f_g$  and  $f_p$  be the mappings given by  $f_g : g_{1,m} \rightarrow$

$(1,m)$  and  $f_p : \otimes_{2^N} \rightarrow (\oplus_2, \oplus_{2^{N-2}})$  where

$g_{1,m} \in G(2^N), 1 \in (0,1), m \in (0,1,2, \dots, 2^{N-2} - 1)$

and  $\square$  is the parallel component-wise operation between any two ordered-pairs  $(1', m')$  and

$(1'', m'')$ , i.e.

$$(1', m') \square (1'', m'') = \left\{ [1' \oplus_2 1''] \right. \\ \left. [m' \oplus_{2^{N-2}} m''] \right\} = (i,j).$$

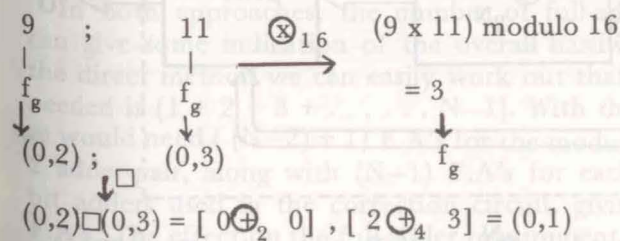
Thus, for any two elements of  $G(2^N)$ , say  $g_{1', m'}$ ,

and  $g_{1'', m''}$ , we have the following useful commutative diagram shown in Fig. 3.

It is now easily seen that the mapping-pair  $f_g, f_p$  transforms the original reduced multiplier into two adders, modulo 2 and modulo  $2^{N-2}$  respectively, operating in parallel.

To illustrate this isomorphism between the multiplier and the adder-pair, let  $N = 4$ . Two possible organisations of  $G(2^4)$  into sets of cosets are (a)  $G(2^4) = \{(1,3,9,11); (7,5,15,13)\}$  and (b)  $G(2^4) = \{(1,7); (3,5); (9,15); (11,13)\}$ .

Consider multiplying, modulo 16, the number 9 by 11. Using the mappings shown in Tables 1 and 2, and the commutative diagram (3), we may substitute additions modulo 2 and modulo 4 for our original modulo 16 multiplication as shown below.



In practice, the results that we have derived are easily applied to the implementation of the general modulo  $2^N$  reduced multiplier. The subgroup K is first generated by simply forming, modulo  $2^N$ , the



successive powers, up to the  $(2^{N-2} - 1)$  th, of 3 or 5, e.g.  $K = 3^0 = 1, 3^1, 3^2, \dots$

$3^{2^{N-2}-1}, 3^{2^{N-2}} = 1$ , either manually or by means of a straight forward computer program for large values of  $N$ . The resulting modulo  $2^{N-2}$  adder may be further structurally simplified using loop-free finite-state machine technique for adders developed by the author (Ref. 3).

### 5. General Comparison With The Direct Implementation of Modulo $2^N$ Multipliers

In making a detailed comparison of our proposed method of implementing a modulo  $2^N$  multiplier with that of the direct approach in which the first  $N$  bits of the partial products are summed using rows of full-adders, the following observations are made.

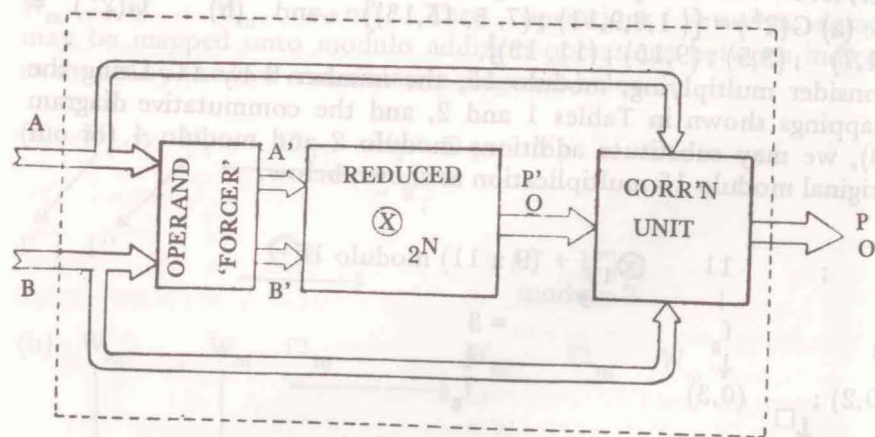


Fig. 1 Block diagram of modulo  $2^N$  multiplication using 'forced' operands and product correction.

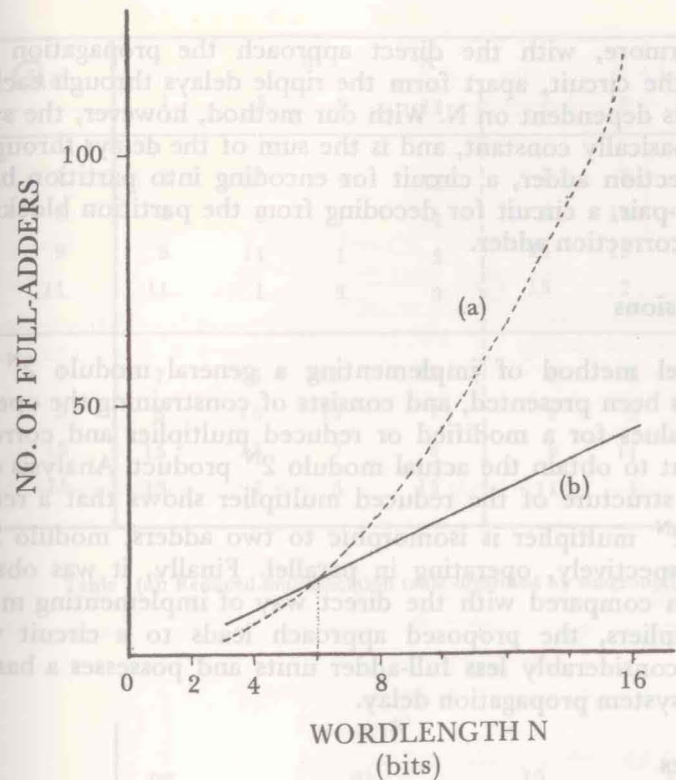


Fig. 2 Complexity in full-adder requirement for (a) direct implementation and (b) proposed implementation of modulo  $2^N$  multiplier.

### Novel implementation method of modulo $2^N$ multiplication

In both approaches, the number of full-adders (F.A.'s) required can give some indication of the overall hardware complexity. With the direct method we can easily work out that the number of F.A.'s needed is  $(1 + 2 + 3 + \dots + N - 1)$ . With the proposed approach, we would need  $(N - 2) + 1$  F.A.'s for the modulo  $2^{N-2}$  and modulo 2 adder-pair, along with  $(N - 1)$  F.A.'s for each of the two  $(N - 1)$ -bit adders used in the correction circuit, giving a total of  $3(N - 1)$  F.A.'s. The effect on the full-adder requirement with increasing wordlength  $N$  is shown in the graph in Fig. 2. We see that with the method proposed, the full-adder count increases linearly with  $N$ , while that of the direct approach is proportional to  $N^2$ . For  $N > 6$ , the proposed implementation technique required considerably fewer full-adders.



Furthermore, with the direct approach the propagation delay through the circuit, apart from the ripple delays through each row of F.A.'s is dependent on N. With our method, however, the system delay is basically constant, and is the sum of the delays through the first correction adder, a circuit for encoding into partition blocks, the adder-pair, a circuit for decoding from the partition blocks, and the final correction adder.

## 6. Conclusions

A novel method of implementing a general modulo  $2^N$  multiplier has been presented, and consists of constraining the operands to odd values for a modified or reduced multiplier and correcting the output to obtain the actual modulo  $2^N$  product. Analysis of the algebraic structure of the reduced multiplier shows that a reduced modulo  $2^N$  multiplier is isomorphic to two adders, modulo  $2^{N-2}$  and 2 respectively, operating in parallel. Finally, it was observed that when compared with the direct way of implementing modulo  $2^N$  multipliers, the proposed approach leads to a circuit which required considerably less full-adder units and possesses a basically constant system propagation delay.

## References

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$\otimes_{16}$	1	3	9	11	7	5	15	13
1	1	3	9	11	7	5	15	13
3	3	9	11	1	5	15	13	7
9	9	11	1	3	15	13	7	5
B'	11	11	1	3	13	7	5	15
7	7	5	15	13	1	3	9	11
5	5	15	13	7	3	9	11	1
15	15	13	7	5	9	11	1	3
13	13	7	5	15	11	1	3	9

Table 1(a). Reduced multiplication table organised by subgroup (1,3,9,11)

$\otimes_{16}$	A'							
	00	01		10		11		
1	1	7	3	5	9	15	11	13
00	1	7	3	5	9	15	11	13
7	7	1	5	3	15	9	13	11
3	3	5	9	15	11	13	1	7
01	5	5	3	15	9	13	11	7
B'	9	9	15	11	13	1	7	3
10	15	15	9	13	11	7	1	5
11	11	11	13	1	7	3	5	9
13	13	11	7	1	5	3	15	9

Table 2(a). Reduced multiplier table organised by subgroup (1,7).

$x_2$	0	1
0	0	1
1	1	0

$x_4$	0	1	2	3
0	0	1	2	3
1	1	2	3	0
2	2	3	0	1
3	3	0	1	2

$x_{16}$	$\oplus_2$
(1,3,9,11)	0
(7,5,15,13)	1

$x_{16}$	$\oplus_4$
(1,7)	0
(9,15)	2
(3,5)	1
(11,13)	3

Table 1(b). Operation between blocks      Table 2 (b). Operation between blocks.

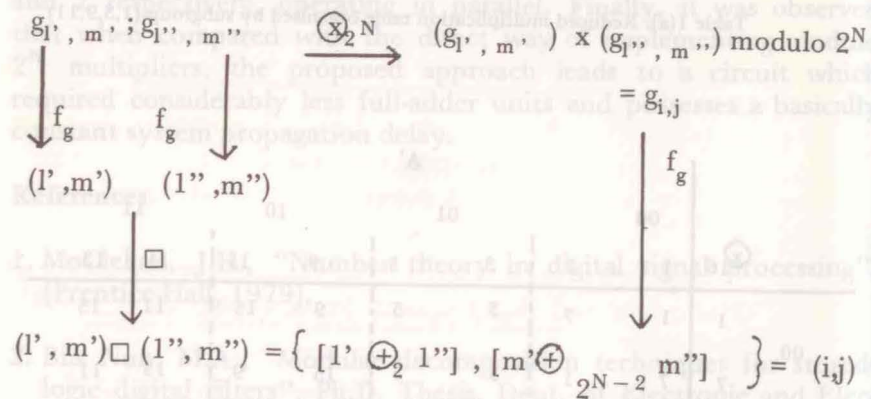


Fig. 3. Commutative diagram for transforming a reduced multiplier modulo  $2^N$  into two adders, modulo 2 and modulo  $2^{N-2}$  respectively, operating in parallel.

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